

# Development of a mathematical model of frequency controlled induction electric drive

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Received 12 May 2021; received in revised form 2 August 2021; accepted 18 August 2021  
DOI <https://doi.org/10.21595/jve.2021.22051>



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**Abstract.** A mathematical model of a frequency-controlled induction (asynchronous) electric drive is proposed, which makes it possible to study electromagnetic and electromechanical processes in an electric drive with any drive mechanism and takes into account the non-sinusoidality of the output voltage of the frequency converter. The block diagram of the algorithms of calculations performed in the “Mathcad” computer application, the results of modeling and their analysis are presented.

**Keywords:** mathematical modeling, induction motor, characteristic, frequency, energy.

## 1. Introduction

At present, the most massive consumers of electrical energy are electric drives based on Induction (asynchronous) electric motors (IM). At the design stages of new and modernization of existing electric drives with IM, an important place is occupied by mathematical modeling of the object [1]. The mathematical description of the electromagnetic and electromechanical processes of an induction electric drive has been known for a long time [2]. Different authors and at different times have used different approaches, methods of analysis, forms of mathematical description of stationary and dynamic modes of operation of induction drive systems [3]. However, the existing models of the electric drive with IM either do not take into account the features of the driven mechanism or designed for one type of mechanisms [5]. So, in, a model of an induction drive for centrifugal mechanisms with a quadratic dependence of the torque resistance on speed is proposed [6]. The authors propose the universalization of the mathematical model of the electric drive in order to use it for mechanisms with any torque resistance. In addition, in the known models, one of the assumptions was the sinusoidality of the supply voltage of the IM. In reality, the output voltage of frequency converters contains higher harmonic components [7-9], leading to distortion of the shape of the motor currents and the electromagnetic torque. The article proposes to supplement the asynchronous motors (AM) model in order to take into account the real form of voltages and currents in a frequency-controlled electric drive [10]. The model, created on the basis of the computer mathematical application “Mathcad”, and this model is quite universal, since it covers all options for IM control. By setting the necessary initial conditions [11], all types of transient processes (start, stop, reverse, load shedding and surge) are modeled, various forms of setting influences for their formation. Calculation of instantaneous values of currents, torques, and powers is accompanied by the calculation of integral characteristics - powers during the transient process, power factors and efficiency [12]. The complete system of initial differential equations describing the processes in the induction electric drive of centrifugal pumps consists of three groups: the equations of electromagnetic equilibrium (Kirchhoff), which describe the electromagnetic processes in the engine, the equations of electromechanical energy conversion, and the equations characterizing the features of the mechanical load on the motor shaft [13-15].



In the proposed model, it has been proposed to unify this calculation by making it applicable for any dependence  $M_c(\omega)$ . The mechanical characteristic of the most mechanisms is a continuous “smooth” function without jumps and discontinuities and, therefore, this can be approximated by a polynomial function [18]. The computer mathematical application “Mathcad” has a number of built-in functions that simplify this solution. One of the is used in the developed model. Let  $M_c$  change during speed regulation according to a nonlinear dependence, uncertain analytically. It is determined experimentally or according to the passport characteristics presented by the manufacturer in the form of graphs or Tables. Fig. 2 shows two such characteristics corresponding to a mechanism with a constant power on the motor shaft ( $M_{c1}$ ) and with a “fan” load ( $M_{c2}$ ).

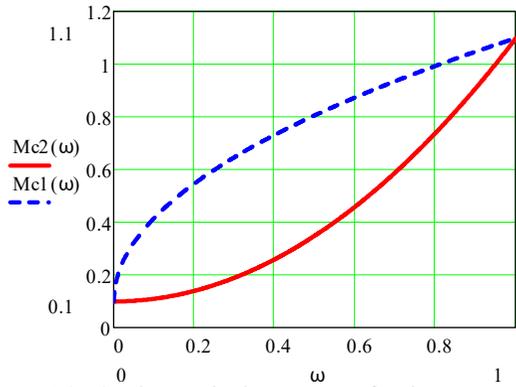


Fig. 2. Changes in the moment of resistance

In the “Calculation of mechanical load” block, the mechanical characteristic presented in the form of a table is converted into a polynomial regression of the form:

$$M_c(\omega) = b_0 + b_1\omega + b_2\omega^2 + \dots + b_n\omega^n. \quad (3)$$

Next, the value of  $dMp/d\omega$  is calculated, which in our case has the form:

$$dM_c(\omega)/d\omega = b_1 + 2b_2\omega + 3b_3\omega^2 + \dots + nb_n\omega^{n-1} \quad (4)$$

Fig. 3 shows a fragment of the program and the results of the calculation in the “Calculation of mechanical load” block for an object with a mechanical characteristic  $M_{c1}$ .

```
Predict mechanical characteristics in polinom (Mathcad 15)
MM1 := ( 0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1 )
      ( 0.1 0.416 0.547 0.648 0.732 0.807 0.875 0.937 0.994 1.049 1.1 )
data := MM1^T X := data<0> Y := data<1> n := rows(data) k := 4
z := regress(X, Y, k) coeffs := submatrix[z, 3, length(z) - 1, 0, 0]
coeffs^T = (0.113 3.36 -7.233 8.207 -3.354)
b0 := coeffs0 b1 := coeffs1 b2 := coeffs2 b3 := coeffs3
b0 := 0,113 b1 := 3,36 b2 := -7,233 b3 = 8.207
Mp(ω) = b0 + b1·ω + b2·ω^2 + b3·ω^3 + b4·ω^4
dMp(ω) = b1 + 2b2·ω + 3b3·ω^2 + 4b4·ω^3
dMp(ω) = d/dω Mp(ω)
```

Fig. 3. Fragment of the program “Calculation of mechanical load”

In the program, the dependence  $M_c(\omega)$  is presented in the form of the MM1 vector. To solve the problem, the program “*regress(X, Y, k)*” is used which built into Mathcad, which returns the vector “*coeffs*” containing the coefficients of the  $k$  degree polynomial, which best approximates the “cloud” of points with coordinates stored in vectors  $X$  and  $Y$ .

Graphical interpretation of the result is shown in Fig. 4. Tabular values of the mechanical characteristics ( $X, Y$ , indicated by crosses) are approximated with high accuracy by the polynomial  $M_p(\omega)$ . The calculated derivative  $dM_p(\omega)$  is also shown here [19].

To obtain the characteristics of any other mechanism in the initial data of the program, it is enough to set the tabular data of its mechanical characteristics. In the figure below (see Fig. 5) the calculation results for the mechanism with the “fan” load  $M_{c2}$  are shown [20].

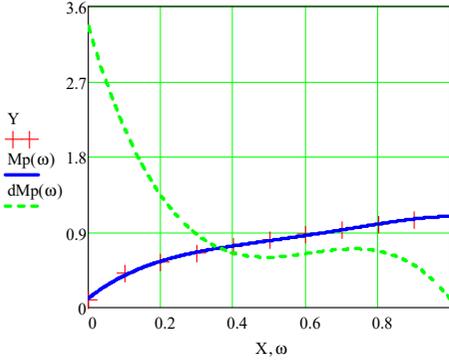


Fig. 4. Exact approximation of the polynomials  $M_p(\omega)$  and  $dM_p(\omega)$

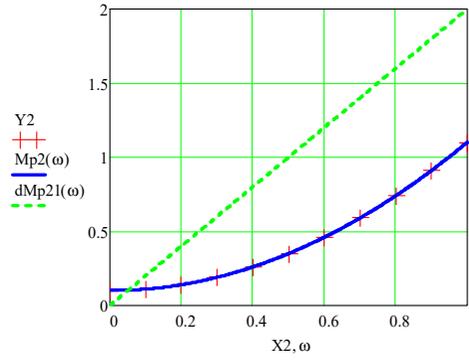


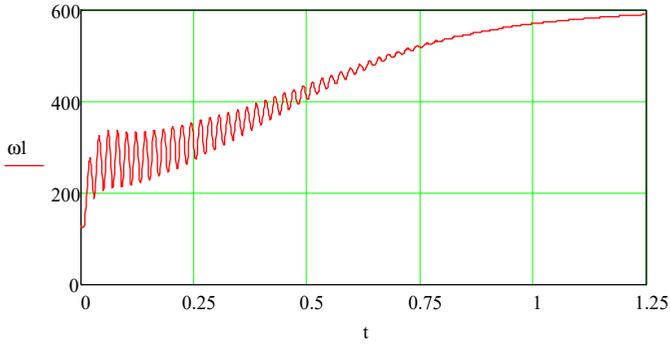
Fig. 5. Fan load moment of resistance

In accordance with the proposed changes, the block for solving the system of differential equations of the mathematical model of an electric drive with IM takes the form:

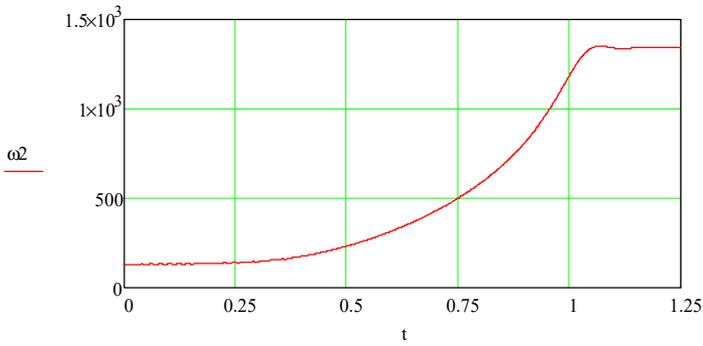
$$\left\{ \begin{aligned} \frac{di_{1x}}{dt} &= \frac{1}{l_1 l_2 - l_m^2} (-r_1 l_2 i_{1x} + \omega l_1 l_2 i_{1y} - \omega s l_m^2 i_{y1} + r_2 l_m i_{2x} \\ &\quad + \omega l_2 l_m i_{2y} - \omega l_2 l_m s i_{2y} + (l_2 u_{1x} - l_m u_{2x})), \\ \frac{di_{1y}}{dt} &= \frac{1}{l_1 l_2 - l_m^2} (-\omega l_1 l_2 i_{1x} + \omega s l_m^2 i_{1x} - r_1 l_2 i_{1y} - \omega l_2 l_m i_{2x} \\ &\quad + \omega l_2 l_m s i_{2x} + r_2 l_m i_{2y} + (l_2 u_{1y} - l_m u_{2y})), \\ \frac{di_{2x}}{dt} &= \frac{1}{l_1 l_2 - l_m^2} (r_1 l_m i_{1x} - \omega l_1 l_m i_{1y} + \omega s l_1 l_m i_{y1} - r_2 l_1 i_{2x} \\ &\quad - \omega l_m^2 i_{2y} + \omega l_1 l_2 s i_{2y} + (l_1 u_{2x} - l_m u_{1x})), \\ \frac{di_{2y}}{dt} &= \frac{1}{l_1 l_2 - l_m^2} (\omega l_1 l_m i_{1x} - \omega s l_1 l_m i_{1x} + r_1 l_m i_{1y} - \omega l_1 l_2 s i_{2x} \\ &\quad + \omega l_m^2 i_{2x} - r_2 l_1 i_{2y} + (l_1 u_{2y} - l_m u_{1y})), \\ \frac{ds}{dt} &= -\frac{3p_n l_m}{2J\omega} i_{1y} i_{2x} + \frac{3p_n l_m}{2J\omega} i_{1x} i_{2y} + \frac{M_c}{J}, \\ \frac{dM_c}{dt} &= \left( \sum b_n s^n \right) \left( \frac{3p_n l_m}{2J\omega} i_{1y} i_{2x} M_n + \frac{3p_n l_m}{2J\omega} i_{1x} i_{2y} M_n s - \frac{M_c}{J} M_n \right). \end{aligned} \right. \quad (5)$$

Fig. 6 and Fig. 7 show the dependences of the torque resistance  $M_{c1}(t)$  and  $M_{c2}(t)$  at the start of the IM, obtained on this model.

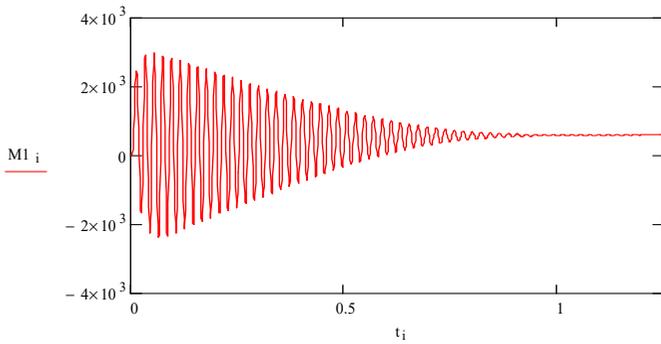
The curves of the IM electromagnetic torque at start-up with various types of loads, obtained on the proposed model, are presented in Fig. 8 and Fig. 9.



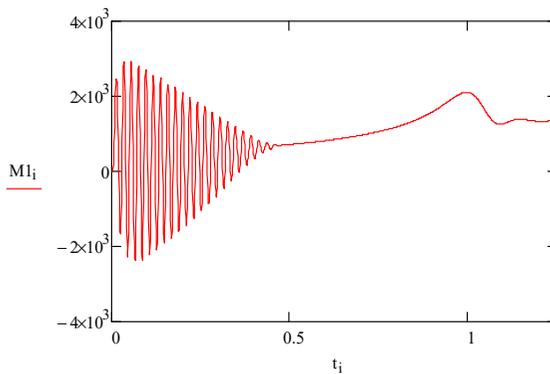
**Fig. 6.** Dependence of the moment of resistances  $M_{c1}(t)$  at the state of the IM



**Fig. 7.** Dependence of the moment of resistances  $M_{c2}(t)$  at the start of the IM



**Fig. 8.** Electromagnetic moment of IM at start with  $M_{c1}$



**Fig. 9.** Electromagnetic moment of IM at start with  $M_{c2}$

### 3. Results and discussion

The obtained curves correspond to the concept of transient processes in an electric drive at the torque resistance of the mechanism, depending on the speed of the motor shaft, as well as to the mechanisms considered in the article (see Fig. 2). The results of simulating a drive with a centrifugal load (Fig. 7-9) coincide with the results obtained in on a model of an induction electric drive of a centrifugal pump [1]. In the previous model, one of the assumptions was the sinusoidality of the supply voltage of the IM. In reality, the output voltage of frequency converters contains higher harmonic components, leading to distortion of the shape of the motor currents and the electromagnetic torque [2]. The article proposes to supplement the IM model in order to take into account the real form of voltages and currents in a frequency-controlled electric drive. For this, the system is supplemented with equations that reflect the output parameters and properties of power supplies [5]. The block diagram adds two blocks (“Frequency converter parameters” and “Calculation of harmonics of the inverter voltage”), in which the harmonic analysis of the inverter output voltage is carried out and the obtained values are converted into synchronous coordinates  $x, y$ . In the calculations, we use the basic concepts of the vector-harmonic method for analyzing electromagnetic processes in IM. It is known that the higher harmonic components of voltages and currents can, like the first harmonics, be represented by vectors rotating with a frequency that is a multiple of the order of harmonics, and, therefore, they can be transformed in different coordinate systems. This makes it possible to use the same algorithms and formulas for calculating the distorting components of motor currents as for calculating electromagnetic processes in IM by the first harmonics. For  $\nu$ -x harmonic components of IM currents and voltages, the equation of electrical equilibrium Eq. (1) retains the structure:

$$\begin{pmatrix} U_{1x\nu} \\ U_{1y\nu} \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} r_1 + p(l_1 + l_m) & -\omega_\nu(l_1 + l_m) & pl_m & -\omega_\nu l_m \\ \omega_\nu(l_1 + l_m) & r_1 + p_n(l_1 + l_m) & \omega_\nu l_m & p_n l_m \\ p_n l_m & -\omega_\nu s_\nu l_m & r_2 p_n(l_2 + l_m) & -\omega_\nu s_\nu(l_2 + l_m) \\ \omega_\nu s_\nu l_m & p_n l_m & \omega_\nu s_\nu(l_2 + l_m) & r_2(l_2 + l_m) \end{pmatrix} \begin{pmatrix} I_{1x\nu} \\ I_{1y\nu} \\ I_{2x\nu} \\ I_{2y\nu} \end{pmatrix}, \quad (6)$$

where  $\nu$  – is the serial number of the harmonic component of current and voltage;  $U_{1x\nu}$  – is the projection of the  $\nu$ -th harmonic of stator voltage on the  $x$ -axis;  $U_{1y\nu}$  – is the projection of the  $\nu$ -th harmonic of the stator voltage onto the  $y$ -axis;  $I_{1x\nu}, I_{1y\nu}$  – is the projections of the  $\nu$ -th harmonic of the stator current, respectively, on the  $x$  and  $y$  axes;  $I_{2x\nu}, I_{2y\nu}$  – is the projections of the  $\nu$ -th harmonic of the rotor current, respectively, on the  $x$  and  $y$  axes;  $l_1, l_2$  – is the phase leakage inductance of the stator and rotor;  $l_m$  – is the inductance of the magnetizing circuit;  $\omega$  – is the angular frequency of rotation of the rotor;  $r_1, r_2$  – is the active resistances of the stator and rotor phases;  $\omega_\nu$  – is the rotation frequency  $\nu$ -th harmonic component.

The difference from the first harmonic equation is as follows [1]. In Eq. (6), the value of  $s_\nu$  appears – slip relative to higher harmonic ones:

$$s_\nu = \frac{\omega_\nu \pm \omega}{\omega_\nu}. \quad (7)$$

In Eq. (7), the minus sign refers to the harmonic components of the positive sequence (including the first harmonic), the plus sign refers to the harmonic negative sequence, the vector of which rotates in the opposite direction.

In the equations of electromechanical energy conversion, the time derivative of  $s_\nu$ :

$$\frac{ds_\nu}{dt} = -\frac{1}{\omega_\nu} \frac{d\omega}{dt} = -\frac{1}{J\omega_\nu} \left( \frac{3p_n l_m}{2} (i_{1y\nu} i_{2x\nu} - i_{1x\nu} i_{2y\nu}) - M_C \right). \quad (8)$$

In the program for calculating the dynamic characteristics of the centrifugal mechanism drive, the quadratic dependence of the moment of resistance on the rotation frequency was used.

One more equation in the system ( $dM_C/dt$  value) is obtained by differentiating the equation of motion of the electric drive with a quadratic dependence of the moment of resistance on the rotation frequency [12]:

$$\frac{dM_C}{dt} = \frac{dM_C}{ds_v} \frac{ds_v}{dt} = (-2M_n + 2M_n s_v) \left[ -\frac{1}{J\omega_v} \left( \frac{3p_n l_m}{2} (i_{1yv} i_{2xv} - i_{1xv} i_{2yv}) - M_C \right) \right]. \quad (9)$$

As a result, taking into account expressions Eqs. (6-9), the system of equations of an asynchronous electric drive takes the form:

$$\begin{cases} \frac{di_{1xv}}{dt} = \frac{1}{l_1 l_2 - l_m^2} (-r_1 l_2 i_{1xv} + \omega_v l_1 l_2 i_{1yv} - \omega_v s_v l_m^2 i_{y1v} + r_2 l_m i_{2xv} + \omega_v l_2 l_m i_{2yv} - \omega_v l_2 l_m s_v i_{2yv} + (l_2 u_{1xv} - l_m u_{2xv})), \\ \frac{di_{1yv}}{dt} = \frac{1}{l_1 l_2 - l_m^2} (-\omega_v l_1 l_2 i_{1xv} + \omega_v s_v l_m^2 i_{1xv} - r_1 l_2 i_{1yv} - \omega_v l_2 l_m i_{2xv} + \omega_v l_2 l_m s_v i_{2xv} + r_2 l_m i_{2yv} + (l_2 u_{1yv} - l_m u_{2yv})), \\ \frac{di_{2xv}}{dt} = \frac{1}{l_1 l_2 - l_m^2} (r_1 l_m i_{1xv} - \omega_v l_1 l_m i_{1yv} + \omega_v s_v l_1 l_m i_{y1v} - r_2 l_1 i_{2xv} - \omega_v l_m^2 i_{2yv} + \omega_v l_1 l_2 s_v i_{2yv} + (l_1 u_{2xv} - l_m u_{1xv})), \\ \frac{di_{2yv}}{dt} = \frac{1}{l_1 l_2 - l_m^2} (\omega_v l_1 l_m i_{1xv} - \omega_v s_v l_1 l_m i_{1xv} + r_1 l_m i_{1yv} - \omega_v l_1 l_2 s_v i_{2xv} + \omega_v l_m^2 i_{2xv} - r_2 l_1 i_{2yv} + (l_1 u_{2yv} - l_m u_{1yv})), \\ \frac{ds_v}{dt} = -\frac{3p_n l_m}{2J\omega_v} i_{1yv} i_{2xv} + \frac{3p_n l_m}{2J\omega_v} i_{1xv} i_{2yv} + \frac{M_C}{J\omega_v}, \\ \frac{dM_C}{dt} = \frac{3p_n l_m}{J\omega_v} i_{1yv} i_{2xv} M_n - \frac{3p_n l_m}{J\omega_v} i_{1yv} i_{2xv} M_n s_v - \frac{3p_n l_m}{J\omega_v} i_{1xv} i_{2yv} M_n + \frac{3p_n l_m}{J\omega_v} i_{1xv} i_{2yv} M_n s_v - \frac{2M_C}{J\omega_v} M_n + \frac{2M_C}{J\omega_v} M_n s_v. \end{cases} \quad (10)$$

Figs. 10-14 show the results of calculations of transient processes taking into account the nonsinusoidality of the output voltage of the inverter by the example of starting an asynchronous motor with a squirrel-cage rotor.

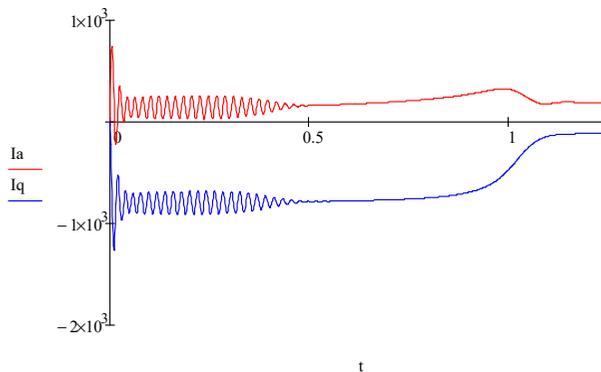
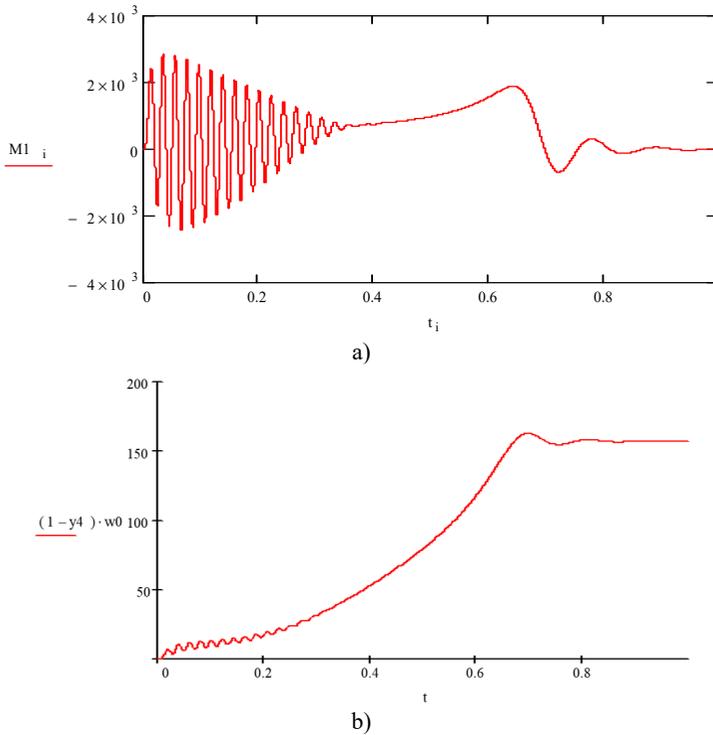


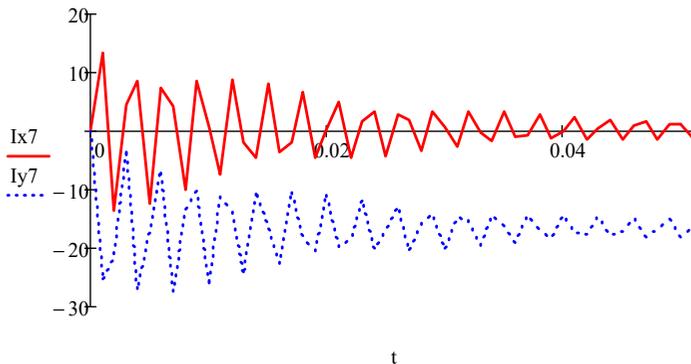
Fig. 10. Active and reactive components of the IM stator current (first harmonics)



**Fig. 11.** a) Speed and b) torque IM (first harmonics)

The curves of the transient process for the first harmonics (see Figs. 2-3) are similar to the results obtained in [1], which confirms the adequacy of the model. For calculations for higher harmonic voltages and currents, a frequency converter with a controlled rectifier, made according to a 6-pulse (bridge) circuit, is adopted [13-15]. The output voltage of such an inverter contains higher harmonic components of the order of:  $\nu = 6n \pm 1$ , where  $n = 1, 2, \dots$

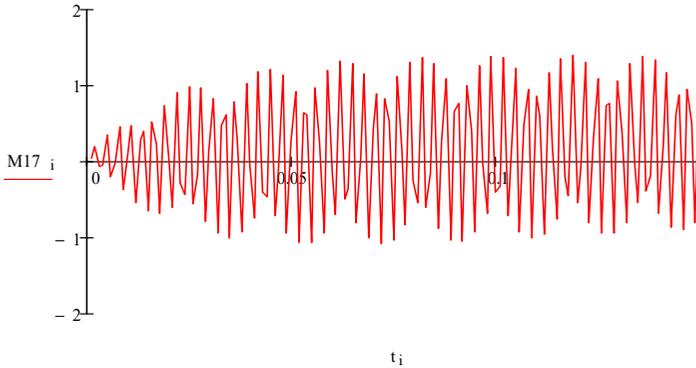
Figs. 4-6 show the results of modeling of transient processes for the seventh harmonics. The frequency and attenuation of the components of the higher harmonics of the stator current of the IM correspond to the well-known concepts of electrical engineering.



**Fig. 12.** Active and reactive components of the AM stator current (seventh harmonic)

Fig. 13 shows the curve of the change in the electromagnetic torque of the IM from the interaction of the seventh harmonics of currents, calculated by the formula:

$$M_7 = \frac{3}{2} p_n L_m (i_{1y7} i_{2x7} - i_{1x7} i_{2y7}). \quad (11)$$



**Fig. 13.** Electromagnetic moment of IM from the interaction of seventh harmonics

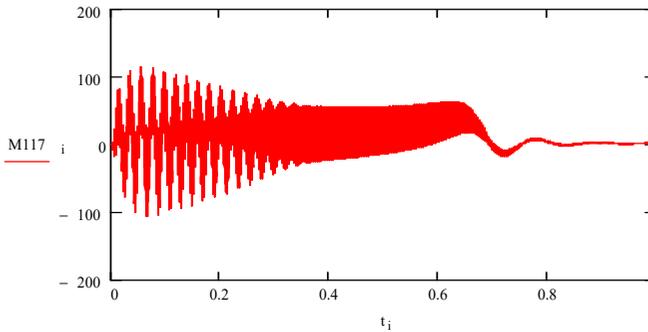
Obviously, the value of such a torque (1.1 Nm) is negligible (the nominal torque of the IM in the model is 1200 Nm). But in the engine, as a result of the interaction of harmonic flux and currents of different orders, pulsating moments are formed [16]. Their main source is the interaction of the main flow with the higher harmonic components of the rotor current:

$$M_{1,\nu} = \bar{\Phi}_1 \cdot \bar{i}_{2\nu},$$

or for the interaction of 1st and 7th harmonics:

$$M_{1,7} = \frac{3}{2} p_n L_m (i_{1y} i_{2x7} - i_{1x} i_{2y7}). \quad (12)$$

The curve of the IM electromagnetic moment calculated according to Eq. (12) is shown in Fig. 6.



**Fig. 14.** Electromagnetic moment of IM from the interaction of the first and seventh harmonics

The amplitude of oscillations of the electromagnetic moment is 115 Nm, i.e. up to 9 % of the nominal value [17, 18]. The total pulsating moment from the interaction of the main flow with all harmonic currents of the rotor can be determined as conclusions:

$$M_{1,\nu} = \frac{3}{2} p_n L_m \sum_{\nu=1}^{\infty} (i_{1y} i_{2x\nu} - i_{1x} i_{2y\nu}).$$

As a result of the further development of the mathematical model of an adjustable induction electric drive, it becomes possible to use the model to study electric drives of mechanisms with any moment of resistance with minimal preparation of data on the load [19]. At the same time, the adequacy of the model is preserved with a high accuracy of representation of the real mechanical characteristics of the driven mechanism, obtained experimentally or from the manufacturer, by a polynomial [20]. The model allows, in addition to options for IM control, types of transient processes, the nature of the load, to take into account the features of the circuit and the principle of operation of the frequency converter.

#### 4. Conclusions

The mathematical model proposed in the article, in addition to the blocks describing electromagnetic and electromechanical processes in an asynchronous motor, includes blocks for calculating the mechanical load and parameters of the frequency converter. The frequency converter (FC) parameter block calculates the harmonic composition of the FC output voltage and prepares data for calculating the highest harmonic components of the IM currents. As a result, the currents and the electromagnetic moment of the IM are calculated taking into account the real (non-sinusoidal) form of the FC voltage. In this case, the calculation is possible for any circuit solution and method of forming the FC voltage. The proposed upgrade allows not only to refine the calculation of the dynamic and static characteristics of the electric drive, but also to assess the impact of the properties of the FC on its energy performance. Taking into account the change in the mechanical load on the motor shaft when adjusting its speed presents significant difficulties. In the proposed model, it is proposed to unify the mathematical description of the mechanical characteristics of the working mechanism. To do this, in the mechanical load calculation block, the entered tabular load data is converted into the coefficients of a polynomial of a given degree, which most accurately approximates the mechanical characteristic of any complexity. The obtained result is further used in solving the equation of motion of the electric drive. As a result, it becomes possible to use the model to study electric drives of mechanisms with any moment of resistance with minimal preparation of load data. Thus, a mathematical model of an adjustable asynchronous electric drive is obtained, which allows, in addition to options for controlling the IM, types of dynamic and stationary processes, to adequately take into account the features of the circuit and the principle of operation of the frequency converter, as well as the features of the mechanical load of any complexity.

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