

Multi-objective rotor dynamics optimization of the plain bearing-rotor system

Xi Kuang¹, Gui-huo Luo², Fei Wang³

College of Energy and Power Engineering, Nanjing University of Aeronautics and Astronautics, Nanjing, 210016, China

²Corresponding author

E-mail: ¹xkuang99@foxmail.com, ²ghluo@nuaa.edu.cn, ³woaijuziyy@gmail.com

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Abstract. The study on rotor dynamics optimization of the plain bearing-rotor system was conducted. In this paper, multi-objective genetic algorithm was used to optimize the weight and stability of a rotor system, so that the stability of the rotor system was improved while the weight was reduced. Compared with single objective optimization, a large number of alternative results could be provided by optimizing one time in the use of the method in this paper. Furthermore, the optimization process can be greatly accelerated with the method, and the method is expected to provide a theoretical basis for improving rotor dynamics optimization of the plain bearing-rotor systems.

Keywords: the plain bearing-rotor system, optimization, multi-objective genetic algorithm.

1. Introduction

Optimization is one of the key methods in the design of a rotor system. The natural frequencies of a rotor system were optimized by Reinhard Helfrich et al. [1], the positions and geometric sizes of the disks, the bearing stiffness and damping were considered as variables. A single-objective optimization problem was proposed by B. S. Yang et al. [2] who used Hybrid G. A. to lower the amplitude of a low-pressure rotor. Actually, besides considering the amplitude and critical speeds, the stability usually should be considered during the design of rotor system [3]. The stability can be changed by lots of optimization variables, so that the sealing of centrifugal pump rotors was optimized by Diewald W. et al. [4, 5], the stiffness of shaft was optimized by Choi B. G. et al. [6].

So far, the research on rotor dynamics optimization is mostly based on single-objective optimization, and multi-objective optimization problems were often transformed into single-objective optimization problems by penalty function method. But as for the design of actual rotor system, it is necessary to consider multiple factors at the same time, and it's often impossible to find only one optimal solution set when multi-objective problem needs to be optimized, so an algorithm that can give a large number of optimal solution sets is valuable. In the meantime, the research on the optimization of rotor system stability is relatively rare. Therefore, the finite element model of the rotor system was established by using the beam elements with shear effect in this paper. After that, the stability and mass of the plain bearing-rotor system were optimized by non-dominated sorting multi-objective genetic algorithm (NSGA-II), this algorithm has the advantage of fast running and good solution convergence.

2. The rotor system model

The model of the plain bearing-rotor system is shown in Fig. 1, the dimension of the model is given in Table 1. The data of disk are given in Table 2. The material parameters of shaft are given in Table 3. The disk was simplified to mass point. The two bearings were located at nodes 11 and 15 respectively. The derivation of inertia matrix and gyro matrix of the disk were directly quoted the conclusions in [7], so do the stiffness matrix and damping matrix of the bearings. As for the plain bearing, we can get the dimensional stiffness and damping coefficient from [8].

The equation of motion of the system is:

$$\mathbf{M}_R \ddot{\mathbf{u}} + (\mathbf{C}_B + \Omega \mathbf{G}_R) \dot{\mathbf{u}} + [\mathbf{K}_R + \mathbf{K}_B] \mathbf{u} = \mathbf{Q}, \quad (1)$$

where R and B represent the rotor and bearing respectively, \mathbf{M}_R is the inertia matrix, \mathbf{K}_R is the stiffness matrix of the rotor, \mathbf{K}_B is the stiffness matrix of the bearing, \mathbf{C}_B is the damping matrix, \mathbf{G}_R is called the gyro matrix, \mathbf{Q} is called the excitation force vector.

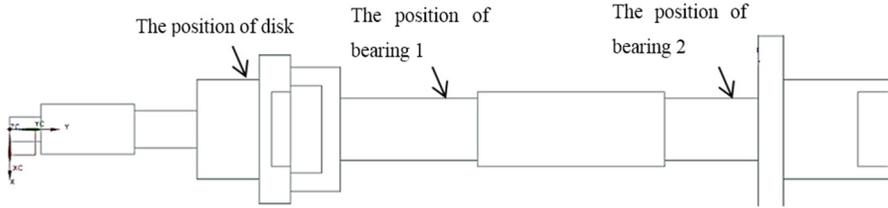


Fig. 1. The model of the rotor system

Table 1. Dimension of the model for the rotor

Node No.	Axial location / m	Element No.	Element length / m	Inner diameter / m	Outer diameter / m
1	0	1	0.0127	0	0.0102
2	0.0127	2	0.0381	0	0.0204
3	0.0508	3	0.0254	0	0.0152
4	0.0762	4	0.0127	0	0.0406
5	0.0889	5	0.0127	0	0.0406
6	0.1016	6	0.0051	0	0.0606
7	0.1067	7	0.0076	0.0304	0.0606
8	0.1143	8	0.0127	0.0356	0.0508
9	0.1270	9	0.0076	0	0.0508
10	0.1346	10	0.0305	0	0.0254
11	0.1651	11	0.0254	0	0.0254
12	0.1905	12	0.0381	0	0.0304
13	0.2286	13	0.0381	0	0.0304
14	0.2667	14	0.0203	0	0.0254
15	0.2870	15	0.0178	0	0.0254
16	0.3048	16	0.0102	0	0.0762
17	0.3150	17	0.0304	0	0.0406
18	0.3454	18	0.0127	0.0304	0.0406
19	0.3581	-	-	-	-

Table 2. The data of disk

Position	Mass / kg	The moment of inertia about diameter / (kg·m ²)	The polar moment of inertia / (kg·m ²)
Node 5	1.401	0.00200	0.00136

Table 3. The data of shaft

Elastic modulus / GPa	Poisson's ratio	Density / (kg/m ³)
207.8	0.3	7806

3. Optimization

For the plain bearing-rotor system in this paper, the optimization of its rotor dynamics can be described by:

$$\begin{aligned} \min f &= [f_1(\mathbf{X}) \quad f_2(\mathbf{X}) \quad \cdots \quad f_N(\mathbf{X})], \\ \text{st. } \mathbf{X}_{LB} &\leq \mathbf{X} \leq \mathbf{X}_{UB}, \end{aligned} \quad (2)$$

where \mathbf{X} is the set of design variables, f_i is the objective functions, \mathbf{X}_{LB} and \mathbf{X}_{UB} represent the boundary of the design variables.

3.1. The objective function

Before optimization, the relationship between rotational speed and the real parts of eigenvalues were given in Fig. 2. It can be seen from Fig. 2 that the real part of the natural frequency line W1 is greater than zero after the rotational speed is greater than 9000 rpm, which means the system is unstable; as for the natural frequency line W2, the unstable state will appear after the rotational speed is greater than 37500 rpm. The natural frequency lines W3 and W4 remain stable throughout the entire speed range. The above statement shows that the plain bearings bring stability problems to the rotor system. Therefore, the stability of the rotor system and the mass of the shaft were optimized in this paper, for the purpose of increasing the speed of each modal enters an unstable state, and reducing the mass of the shaft elements.

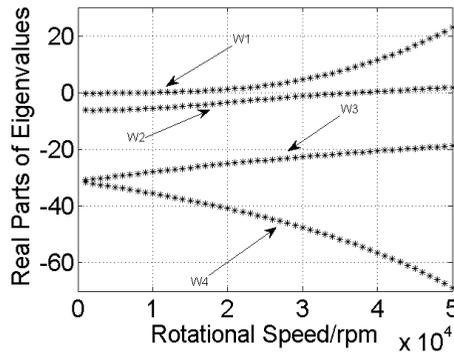


Fig. 2. Real parts of the eigenvalues before optimization

The objective functions can be defined as:

$$\begin{aligned} \min f_1 &= \begin{cases} (W_{max} - \omega_u)/W_{max}, & \omega_u < W_{max}, \\ 0, & \omega_u \geq W_{max}, \end{cases} \\ \min f_2 &= m(\mathbf{X}), \end{aligned} \quad (3)$$

where ω_u is the minimum rotational speed of each modal enters unstable state, $W_{max} = 50000$ rpm is the maximum rotational speed of the rotor system, $m(\mathbf{X})$ represents the mass of entire shaft elements.

3.2. The design variables and constraints

The outer diameter of each shaft element was considered as the design variables:

$$\mathbf{X} = [d_1 \quad d_2 \quad \dots \quad d_{18}], \quad (4)$$

where d_i is the outer diameter, and the constraints are:

$$0.01 \text{ m} \leq d_i \leq 0.1 \text{ m}, \quad i = 1, 2, 3 \dots 18. \quad (5)$$

The radial clearances of the plain bearings, c_1 and c_2 , were also used as design variables due to their greater influence in rotor dynamics. The related parameters of the plain bearings are: the coefficient of kinetic viscosity is $\mu = 2.6502 \times 10^{-2}$ Pa·s, the effective length of bearing is $L = 0.008$ m. Before optimization, the radial clearances are $c_1 = c_2 = 5 \times 10^{-6}$ m, the mass of entire shaft elements is 5.4886 kg.

4. Results

The relationship between the objective functions after optimization is shown in Fig. 3. f_1 is the stability of rotor system, f_2 is the mass of entire shaft elements. It can be seen that each individual result is better than original results, $f_1 = 0.82$ and $f_2 = 5.4886$.

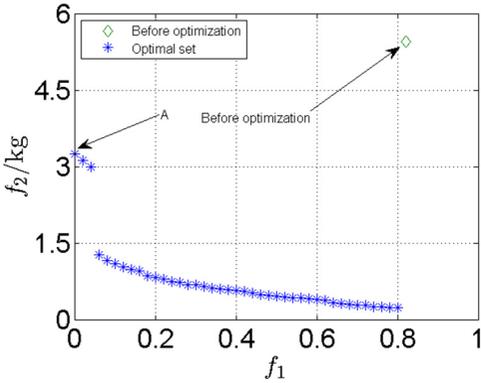


Fig. 3. Optimization results for complex rotor system

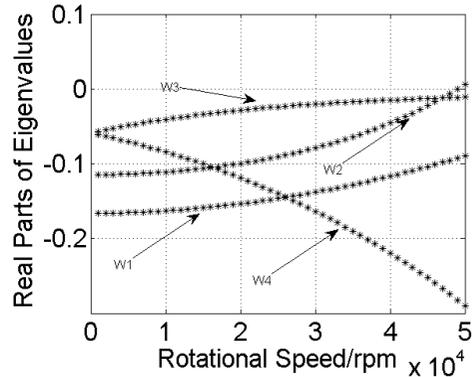


Fig. 4. Real parts of eigenvalues for individual A

The real parts of eigenvalues for individual A in Pareto front is shown in Fig. 4. Individual A means that the stability is the best, whereas its mass is biggest. Individual A isn't the most suitable choice in most cases for the designers, people still need to choose the only solution from the Pareto front. The simplest method is the reference point method [9]. There are many methods can be used to select suitable individual from the Pareto front. The reference point method is the only one of them. Deeply discussion of these methods is not the focus of this paper, so only the reference is listed here [10].

5. Conclusions

In this paper, the model of the rotor system was established by the finite element method, and the optimization of weight and stability for the rotor system was carried out by multi-objective genetic algorithm.

The research shows that:

- 1) Multiple optimal solutions can be given by NSGA-II algorithm, and there is no dominant relationship between any two individuals in these solutions. Therefore, a large number of alternatives can be provided through only one optimization in the rotor system design stage.
- 2) The stability of the rotor system with plain bearings and the weight of the shaft element had been successfully optimized, which improves the stability of the rotor system and greatly reduces the total mass of the rotor system.

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