1373. Structural synthesis for broken strands repair operation metamorphic mechanism of EHV transmission lines

Q. Yang1, H. G. Wang2, S. J. Li3
1, 3College of Mechanical Engineering and Automation, Northeastern University Shenyang, Liaoning, 110004, P. R. China
1, 2, 3State Key Laboratory of Robotics Shenyang, Liaoning, 110016, P. R. China
3Corresponding author
E-mail: 1 qiangyang@mail.neu.edu.cn, 2 hgwang@sia.ac.cn, 3 shjunli@mail.neu.edu.cn
(Received 8 August 2014; received in revised form 16 August 2014; accepted 22 August 2014)

Abstract. Special operation requirements are needed for repositing broken strands of extra-high-voltage (EHV) power transmission lines before repairing. Metamorphic mechanism is applied to satisfy the requirements and a novel structural synthesis method is proposed, considering the forms and structures of constrained metamorphic joints. Metamorphic cyclogram and equivalent resistance gradient matrix of metamorphic joints are obtained by analyzing the repairing operation. Meanwhile, the source metamorphic mechanism with structure of non-constrained metamorphic joints is selected. Constrained form/structure matrix of metamorphic joints is built according to metamorphic cyclogram and equivalent resistance gradient matrix. The relation between constraint force changes of joints and form/structure of metamorphic joints is then obtained; and all the eight corresponding structures of constrained metamorphic mechanism are synthesized. One of the eight mechanisms is chosen as the broken strands reposition metamorphic mechanism, and its topological transformations of working configuration are analyzed to verify the feasibility and practicality of structural synthesis method proposed in this paper.

Keywords: metamorphic mechanism, structural synthesis, forms/structures of metamorphic joints, topological transformation, broken strands repair operation.

1. Introduction

Broken strands repairing operation of EHV power transmission lines is one of the most important maintenance work of grid. At present, the most common way of repairing is still manually done by line workers on live-line, which is dangerous, costly and inefficient. In order to accomplish long-term maintenance operations and immediate repairing operations for broken lines, a live-line work mobile robot is urgently needed for the special operation condition. To develop the mobile robot repair/maintain system is one of the most available ways to solve the problems with efficiency and lower cost. The study of broken strands live-line repairing operation is still under development. The broken strands maintenance robot system was developed by IREQ in Canada 2005, and the LineScout can repair the broken strands of power transmission lines in live-line [1-2]. Currently, international researchers have done some work on live-line inspection robot to establish a research foundation for the broken strands repair robot system [3-8]. The system consists of a mobile robot and broken strands operation mechanism. Broken strands (Fig. 1(b)) must be repositioned to the original form (Fig. 1(a)) before repairing. The development of broken strands reposition mechanism is one of the most important work for live-line repairing operation of EHV power transmission lines.

Metamorphic mechanism, which was first proposed a decade ago, is a variable mobility, changeable topology mechanism [9-10]. According to the required working stages and working sequences, metamorphic mechanism can change its topology to satisfy different requirements and achieve under-actuated operation by constraining the metamorphic joints of the mechanism alternately. This is based on kinematic geometry arrangements, geometric and/or force constraints, designated profiles of links and/or joints, etc [11-12]. At present, structural synthesis study of the
metamorphic mechanism is more concentrated on source metamorphic mechanism and its topological transformation [13-15]. That lacks the research on obtaining forms/structures of constrained metamorphic joints and all the corresponding metamorphic configurations according to the same source metamorphic mechanism, especially structural synthesis method of practical constrained metamorphic mechanism in the special operation condition. According to the special operating and technology background of the broken strands repair process, a 2-DOF metamorphic mechanism is selected as the broken strands reposition mechanism, considering the demand of multi-mobility, under-actuated operation, specific motion requirements, and the special operation condition. Based on the changing of resistance in the metamorphic process [16], a structural synthesis method is proposed to determine the constrained forms/structures of metamorphic joints and all the corresponding metamorphic mechanisms. This research provides a reference for the structural synthesis study of practical metamorphic mechanisms.

Fig. 1. a) Normal strands, b) broken strands

2. Operating condition

For the broken strands repair robot of EHV power transmission lines, broken strands reposition component is a kind of repositioning nut with rolling element in its inner wall, which sleeves EHV transmission lines and makes the rolling element embed into the gap between adjacent strands. The process of broken strands repositioning is equivalent to the meshing course between the repositioning nut pushed by a mobile robot and the strands, which will complete broken strands reposition operation of lines. Because EHV transmission lines are closed, the repositioning nut must be made of two cut-open nuts as shown in Fig. 2(a), which would clamp the live-line and be locked into a unite one (Fig. 2(b)) to prevent the cut-open nuts from bulging open while the mobile robot pushes them moving along the line during the broken strands reposition operation.

Fig. 2. The cut-open nut

3. Design of source metamorphic mechanism

3.1. Operational requirements

According to the operating requirements, the reposition mechanism must be designed with 2 DOFs. One DoF is the motion of making two cut-open nuts clamp EHV power lines, the other is the motion of locking the two cut-open nuts into a united one through pins. Because of the special operation condition, it is required to reduce the weight of repair mobile robot, to simplify the control system, and to save the carrying energy (usually lithium battery). Therefore, 2-DOF constrained metamorphic mechanism is designed as the reposition mechanism which completes the two motions above with only one driver.
3.2. The design of source metamorphic mechanism

In accordance with the kinematic requirements and operating condition, the metamorphic mechanism is designed with 2 DOFs and two rotational constrained metamorphic joints. Metamorphic processes are achieved during the configuration transforming. The working statuses of constrained metamorphic joints will transfer between moving and static dependent on the changing of constrained forces to form the corresponding working stages, while the diver joint and general joints keep working. The displacement (turning angle or moving distance) $\theta$ of the driver is shown in horizontal axis, and the working conditions of joints $J$ ($J = R$ for revolute joint, $J = P$ for prismatic joint etc.) in corresponding working stages (or metamorphic configurations) is shown in vertical axis. The working configuration transferring and the working statuses of metamorphic joints can be described in metamorphic cyclogram as shown in Fig. 3 [16], which shows the working statuses of all the joints with the movement of driver in the corresponding working stages. Finally, the metamorphic cyclogram of 2-DOF reposition metamorphic mechanism is obtained as shown in Fig. 3. Configuration I and Configuration II denote two working configurations of the metamorphic mechanism. Suppose the driving link obtains translational motion of screw driven by a motor, a kind of corresponding planar 5-bar mechanism, i.e. source metamorphic mechanism is designed as shown in Fig. 4.

<table>
<thead>
<tr>
<th>J</th>
<th>Configuration I</th>
<th>Configuration II</th>
</tr>
</thead>
<tbody>
<tr>
<td>$J_1(P_{13})$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$J_3(R_{13})$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$J_4(R_{34})$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$J_5(R_{54})$</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

![Fig. 3. Metamorphic cyclogram of the metamorphic mechanism](image)

![Fig. 4. The source metamorphic mechanism of broken strands reposition](image)

4. Structural synthesis method of constrained metamorphic mechanism

4.1. Equivalent resistance gradient sketch of metamorphic joints

Based on Fig. 3 and equivalent resistance gradient model proposed in reference [16], the equivalent resistance gradient sketch of constrained metamorphic mechanism (Fig. 4) is obtained as shown in Fig. 5, in which $f_e$ denotes equivalent resistance coefficient and $\theta$ denotes the displacement of the driver.

The equivalent resistance gradient sketch of metamorphic joints can be described as matrix, i.e. the equivalent resistance matrix:

$$
F = \begin{bmatrix}
0 & f_{45} \\
 f_{34} & 0
\end{bmatrix},
$$

(1)
where, working configurations are shown in columns of the matrix, constrained status of metamorphic joints with different working configurations are shown in rows, and $f_{ij}$ denotes that metamorphic joint $R_{ij}$ keeps constrained, 0 means $R_{ij}$ keeps working.

4.2. The structural topology matrix of constrained metamorphic mechanism

4.2.1. Constrained metamorphic joints

Typical constrained structures and constrained matrixes of metamorphic joints are shown in Fig. 6. Fig. 6(a) shows the turning joint and prismatic joint with geometric constraint which overlaps two links into one and provides infinite constraint force at the point. Fig. 6(b) shows the turning joint and prismatic joint with spring force constraint. Fig. 6(c) shows the turning joint and prismatic joint with geometric constraint controlled by spring which provides limited constraint force at the point. Fig. 6(d) shows the turning and prismatic joints with geometric constraint and spring force constraint respectively. Fig. 6(e) shows the turning and prismatic joints with geometric constraint and geometric constraint controlled by spring respectively. In constrained matrixes, 0 denotes that metamorphic joint $R_{ij}$ keeps moving and 1 denotes that $R_{ij}$ keeps static.

Suppose $g = r, p$ which denotes revolving or prismatic metamorphic joints with geometric constraints. $s = rk, rt, pk, pt$, where $rk$, $rt$ denote revolving metamorphic joints with spring force constraint and geometric constraint controlled by spring respectively, and $pk, pt$ denote prismatic metamorphic joints with spring force constraint and geometric constraint controlled by spring respectively. $sg = rk_g, rt_g, pk_g, pt_g$, which denotes metamorphic joints (revolving or prismatic) with spring force constraint and geometric constraint, and with geometric constraint and geometric constraint controlled by spring.

Fig. 6. Typical constrained structures of metamorphic joints
4.2.2. The structural topology matrix of constrained metamorphic mechanism

In order to build the connection between constrained structures of metamorphic joints and its equivalent resistance matrixes in corresponding with working stages, structural topology matrix $C$ of constrained metamorphic mechanism and constrained structures matrix $R_{ij}$ of constrained metamorphic joints are built:

\[
C = \begin{bmatrix}
R_{45} \\
R_{34}
\end{bmatrix} = \begin{bmatrix}
0 & c_{45} \\
c_{34} & 0
\end{bmatrix}.
\]

In matrix $C$, working configurations are shown in columns and constrained structures matrix $R_{ij}$ of metamorphic joints are shown in rows. Compared the rows of Eq. (2) with constrained structures of Fig. 6, constrained structures matrix of metamorphic joints can be deduced:

\[
R_{45} = [g/st],
\]

\[
R_{34} = [sk/st/rkg/rtg].
\]

Taking Eq. (3) into Eq. (2), structural topology matrix of constrained metamorphic mechanism is obtained:

\[
C = \begin{bmatrix}
R_{45} \\
R_{34}
\end{bmatrix} = \begin{bmatrix}
0 & c_{45} & r/rt \\
c_{34} & 0 & 0
\end{bmatrix} = \begin{bmatrix}
k/rk/rt/rkg/rtg & 0
\end{bmatrix}.
\]

According to Eq. (4) and permutations and combinations theory, the eight structural topology matrices can be calculated as:

\[
C_1 = \begin{bmatrix}
0 & r \\
k/rt & 0
\end{bmatrix}, \quad C_2 = \begin{bmatrix}
0 & r \\
rt & 0
\end{bmatrix}, \quad C_3 = \begin{bmatrix}
0 & r \\
rkg/rt & 0
\end{bmatrix}, \quad C_4 = \begin{bmatrix}
0 & r \\
r/rtg & 0
\end{bmatrix},
\]

\[
C_5 = \begin{bmatrix}
0 & rt \\
k/rt & 0
\end{bmatrix}, \quad C_6 = \begin{bmatrix}
0 & rt \\
rt & 0
\end{bmatrix}, \quad C_7 = \begin{bmatrix}
0 & rt \\
rkg/rt & 0
\end{bmatrix}, \quad C_8 = \begin{bmatrix}
0 & rt \\
r/rtg & 0
\end{bmatrix}.
\]

There are eight constrained structures of metamorphic joints together, which means eight corresponding constrained metamorphic mechanisms can be designed theoretically to satisfy broken strands reposition operation.

4.3. Structural diagram of constrained metamorphic mechanism

According to the structural topology matrix $C_i$ ($i = 1, 2, \ldots, 8$), the eight structural diagrams of reposition metamorphic mechanisms are illustrated in Fig. 7.

5. Structural design and working configurations analysis of the reposition constrained metamorphic mechanism

5.1. Design of the practical reposition metamorphic mechanisms and its topological transformations

The selection of the structural form is based on the reliable working configuration transforming ability and the structure simplicity. In this point of view, the mechanisms of Fig. 7(c) and Fig. 7(d) can both achieve reliable metamorphic process in metamorphic joint C. Fig. 7(c) mechanism is selected as the practical broken strands reposition metamorphic mechanism because the structure of joint C is simpler than that of Fig. 7(d). The mechanisms of Fig. 7(e)-(h) are ignored, because the form combinations of metamorphic joints with spring force constraint and geometric constraint controlled by spring are less reliable in the configuration transforming than that of Fig. 7(c). The
joints C in mechanisms of Fig. 7(a) and Fig. 7(b) only have spring force constrains (no geometric constrains), which make them deselected. The mechanism in Fig. 7(c) is selected as the practical broken strands reposition metamorphic mechanism. Metamorphic joint C is spring force constraint and geometric constraint, and D is geometric constraint. Considering the symmetrical operation of practical mechanism, the practical broken strands reposition metamorphic mechanism is finally designed (Fig. 8).

![Fig. 7. Structural diagrams of reposition metamorphic mechanisms](image)

This mechanism mainly consists of 2 parts, a main clamping metamorphic mechanism and a locking mechanism. The main clamping mechanism is a 5-bar metamorphic mechanism, which is comprised of screw nut 1, link 2, link 3, clamp 4 and the frame 0 in x-y plane (Fig. 8(a)). Cut-open nut 11 is embedded in clamp 4, and spring 10 and a geometric structure constrains joint C, and the geometric limitation (strand 12) constrains pair D. This mechanism can provide 2 motions, one for carrying two cut-open nuts clamping EHV power lines, and the other for providing driving motion (link 3) for the locking mechanism below.

The locking mechanism is made up of crank 6, link 7, slider 8 and the frame 0 in x-z plane, which actually is a crank-slider mechanism, as is shown in Fig. 8(b). It can provide the motion of locking the two half cut-open nuts into a united one through pins. The main clamping mechanism
and locking mechanism are connected through a pair of bevel gears 3’ and 6’, which are rigidly connected to link 3 and crank 6 respectively. Pin 9 is a joining pin used to lock the two half cut-open nuts, while the pin on the other side is just part of slider 8’ used to disassemble the united nut after the repairing operation.

5.2. The working configurations analysis of metamorphic process

The reposition metamorphic mechanism proposed will be carried by a mobile robot and mounted onto the EHV power line. In its initial working configuration (Fig. 9), link 3 and clamp 4 are fixed together by spring 10 and a special geometrical constraint.

When operation starts, screw 5 rotates driven by a motor, and screw nut 1 moves towards the symmetrical centre, which drives clamp 4 to swing around D to carry the cut-open nut 11 to clamp and tighten the EHV power line 12, as shown in Fig. 9.

![Fig. 9. The configuration of changing work stage](image)

When clamping operation is finished, clamp 4 will be fixed as a part of the frame. Along with the motion of screw nut 1, link 3 begins to rotate around joint C after overcoming the spring resistance to provide a driving motion for the locking mechanism as shown in Fig. 10.

Beginning to rotate around joint C, link 3 drives bevel gear 3’ (Fig. 8(b)) to rotate relative to clamp 4 in x-z plane. Through the bevel gears 3’ and 6’ (Fig. 8(b)), movement and power are transferred to the locking mechanism which moves along with crank 6, and makes slider 8 move toward the cut-open nuts. Pin 9 connects the two cut-open nuts into a united one. The motor rotates inversely, so slider 8 moves toward the opposite direction, and joining pin 9 will remain in the pin hole. While on the right side, pin 9’ will move with slider 8’ retreating from the corresponding hole, and then the locking operation is finished. After moving back to the initial configuration, the united cut-open nut meshes with the strands to perform the reposition operation. The disassemble operation of the united cut-open nut will be done by the mechanism when the mobile robot pushes the nut to a position where the nut’s phase angle is 180°relative to the initial orientation.

6. Kinematic analysis and computational simulation

6.1. Main kinematic structure size

Table 1 shows the designed key structural parameters of the broken strands reposition metamorphic mechanism.
Table 1. Kinematic parameters of the mechanism

<table>
<thead>
<tr>
<th>Quantity</th>
<th>( L_0 )</th>
<th>( L_2 )</th>
<th>( L_3 )</th>
<th>( L_4 )</th>
<th>( L_6 )</th>
<th>( L_7 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value (mm)</td>
<td>15</td>
<td>120</td>
<td>25</td>
<td>80</td>
<td>25</td>
<td>35</td>
</tr>
</tbody>
</table>

Where \( L_i \) denotes the length of link \( i \), \( L_0 \) represents the vertical distance from the centre of joint D to the centre of screw 5.

6.2. Position analysis of the mechanism

6.2.1. Position analysis of the main metamorphic mechanism

Fig. 11 shows the vector diagram of the main mechanism, which is a 5-bar metamorphic mechanism in \( x-y \) plane. A closed loop vector equation can be deduced:

\[
S_1 + L_0 + L_4 + L_3 = L_2,
\]

(5)

where, \( S_1 \) is the position of slider 1. Eq. (6) can be derived according to the geometrical relationship:

\[
\begin{align*}
\theta_4 &= 90^\circ + \arctan \frac{S_1}{L_0} + \arcsin \frac{L_3}{\sqrt{L_0^2 + L_4^2 - 2L_0L_4 \cos \theta_4}} \\
&+ \arccos \frac{L_3^2 + L_4^2 - 2L_0L_4 \cos \theta_4 + S_1^2 + L_0^2 - L_3^2}{2 \sqrt{S_1^2 + L_0^2 + L_4^2 - 2L_0L_4 \cos \theta_4}},
\end{align*}
\]

(6)

where \( \theta \) denotes the location angle of link. When the mechanism keeps in configuration I, \( \theta_3 \) and \( \theta_4 \) will be fixed relatively, and \( \theta_{43} = \theta_4 - \theta_3 = 75^\circ \). However, when the mechanism keeps in configuration II, clamp 4 will be fixed as a part of the frame which means \( \theta_4 \) becomes a constant \((255^\circ)\). Thus \( \theta_3 \) can be calculated as:

\[
\begin{align*}
\theta_3 &= 90^\circ + \arctan \frac{S_1 + L_4 \cos \theta_4}{L_0 - L_4 \sin \theta_4} \\
&+ \arccos \frac{L_3^2 + S_1^2 + L_0^2 + L_4^2 + 2(S_1L_4 \cos \theta_4 - L_0L_4 \sin \theta_4) - L_3^2}{2L_3 \sqrt{S_1^2 + L_0^2 + L_4^2 + 2(S_1L_4 \cos \theta_4 - L_0L_4 \sin \theta_4)}},
\end{align*}
\]

(7)

6.2.2. Position analysis of locking mechanism

Fig. 12 shows the vector diagram of the locking mechanism, which is a crank-slider mechanism in \( x-z \) plane. A closed loop vector can be calculated as:

\[
L_6 + L_7 = S_8.
\]

(8)

Eqs. (9) and (10) are deduced according to the geometrical relationship:

\[
\begin{align*}
S_8 &= L_6 \cos \theta_6 + \sqrt{L_7^2 - L_6^2 \sin^2 \theta_6}, \\
\theta_6 &= \theta_{60} + \frac{\theta_3 - 180^\circ}{i_{3/6}},
\end{align*}
\]

(9, 10)

where, \( \theta_{60} = 40.5358^\circ \) which is the initial location angle of the crank, as is shown in Fig. 12. \( i_{3/6} = 0.7 \), which is the transmission ratio of the bevel gear pair. According to the Eqs. (5) to (10), the relationship between \( S_1 \) and \( S_8 \) can be obtained, as well as functional relationships of angle \( \theta_3 \), \( \theta_4 \) and position of the slider \( S_8 \) against \( S_1 \), as shown in Fig. 13. The values in key points are listed in Table 2.
6.3. Simulation

Practical metamorphic process (1 to 4) is simulated with a 3D modelling software package (Solidworks 2010).

1) The initial configuration of the mechanism which is carried by a mobile robot and mounted onto EHV power line is shown in Fig. 14.

2) The configuration of clamp 4 (two clamps) which carries the cut-open nuts clamping the EHV power line is shown in Fig. 15.

3) During the working Configuration II, link 3 drives bevel gears and locking mechanism to insert the pins into the holes of cut-open nuts for connecting the two cut-open nuts as a united one, as is shown in Fig. 16.

4) Slide 1 moves back and joining pins remains in the pin holes of the cut-open nuts to keep two cut-open nuts as a united one, as shown in Fig. 17. The mechanism moves back to the initial configuration, and the mobile robot can push the united nut to mesh with power transmission lines for the broken strands reposition operation, as shown in Fig. 18.

Table 2. The key kinematic parameters transforming from Configuration I to Configuration II

<table>
<thead>
<tr>
<th>Configuration</th>
<th>( S_1 ) (mm)</th>
<th>( \theta_4 ) (°)</th>
<th>( \theta_5 ) (°)</th>
<th>( \theta_6 ) (°)</th>
<th>( S_8 ) (mm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Configuration I</td>
<td>155.50-122.42</td>
<td>240-255</td>
<td>165-180</td>
<td>40.5358</td>
<td>50</td>
</tr>
<tr>
<td>Transforming</td>
<td>122.42</td>
<td>255</td>
<td>180</td>
<td>40.5358</td>
<td>50</td>
</tr>
<tr>
<td>Configuration II</td>
<td>122.42-109.27</td>
<td>255</td>
<td>180-200</td>
<td>40.5358-69.0752</td>
<td>50-34.98</td>
</tr>
</tbody>
</table>

Fig. 14. The initial configuration of the mechanism

Fig. 15. The cut-open nuts clamping the EHV line
7. Conclusions

According to the special operation requirements, and the application condition of broken strands repair mobile robot used in EHV power transmission lines, a practical structural synthesis method for metamorphic mechanism is proposed. Applying the method, all the eight theoretical structures of the reposition metamorphic mechanism and forms/structures of constrained metamorphic joints are obtained. Finally, the reposition metamorphic mechanism designed can achieve multi-mobility with single-drive, which reduces the weight of the robot and save the energy carried. The results indicate that the method provides a novel way for designing broken strands repair operation mechanism of EHV power transmission lines, also for the similar design requirements of under-actuated mechanisms.

Acknowledgement

The authors would like to acknowledge the financial support of the State Key Laboratory of Robotics of China (2012-O16), and the National Natural Science Foundation of China (Grant No. 51175069, 51205052).

References


Qiang Yang received the BS degree in Mechanical Engineering from Shenyang Jianzhu University, China, in 2003, and his MS and PhD degrees in Mechanical Engineering from Northeastern University, China, in 2005 and 2009, respectively. He is a lecturer in School of Mechanical Engineering and Automation, Northeastern University. His research interests include theory of mechanisms, metamorphic mechanisms, parallel mechanisms, and kinematic reliability of mechanisms.

Hongguang Wang is a professor in State Key Laboratory of Robotics, Shenyang Institute of Automation and Chinese Academy of Sciences. His current research interests include the analysis and synthesis of robot mechanism, the mechanics of serial and parallel manipulators, the modular reconfigurable robots and autonomous mobile robots.

Shujun Li is a professor in School of Mechanical Engineering and Automation, Northeastern University, China. His research interests include theory of mechanisms, theory of robot mechanisms, metamorphic mechanisms, and mechanical design theory and method.